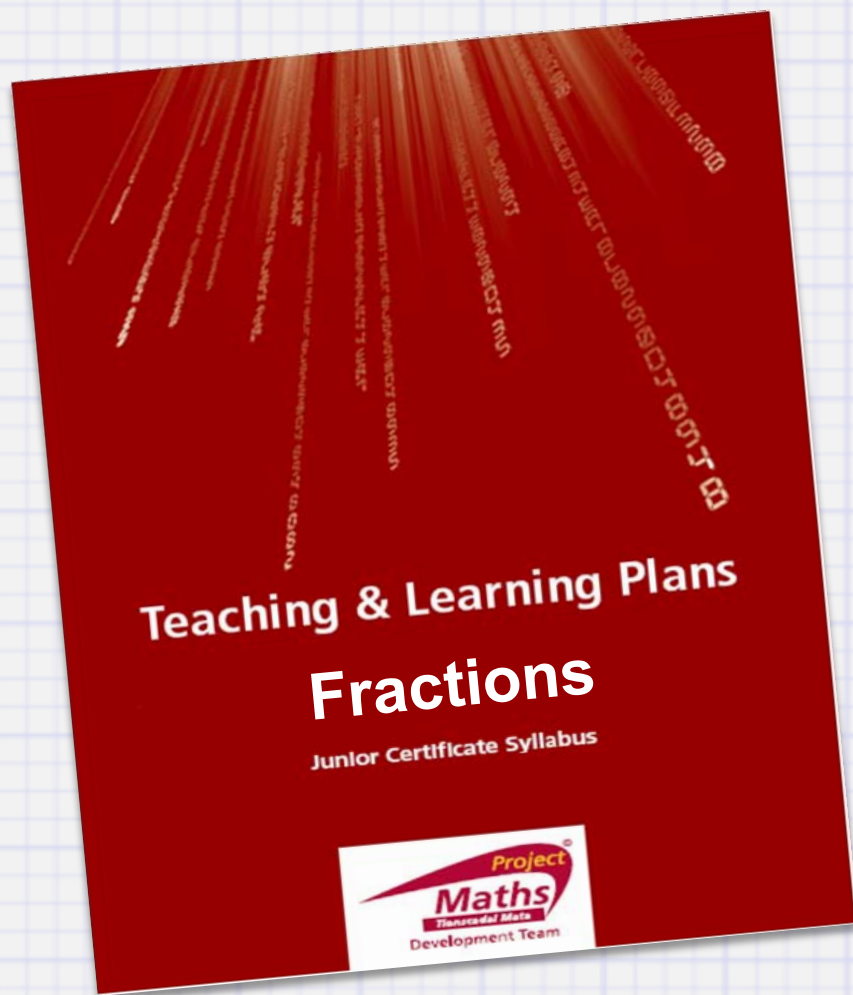


# Strand 3: Number



# Fractions are Easy!

- Half a cup of tea
- Quarter of an hour
- Three quarters full



*Point to Ponder!*

$$\frac{2}{3} \text{ of } \frac{4}{5} = ?$$

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# Lesh's Translation Model

Pictures

Spoken  
Symbols

Manipulative  
Models

Real Life  
Situations

Written  
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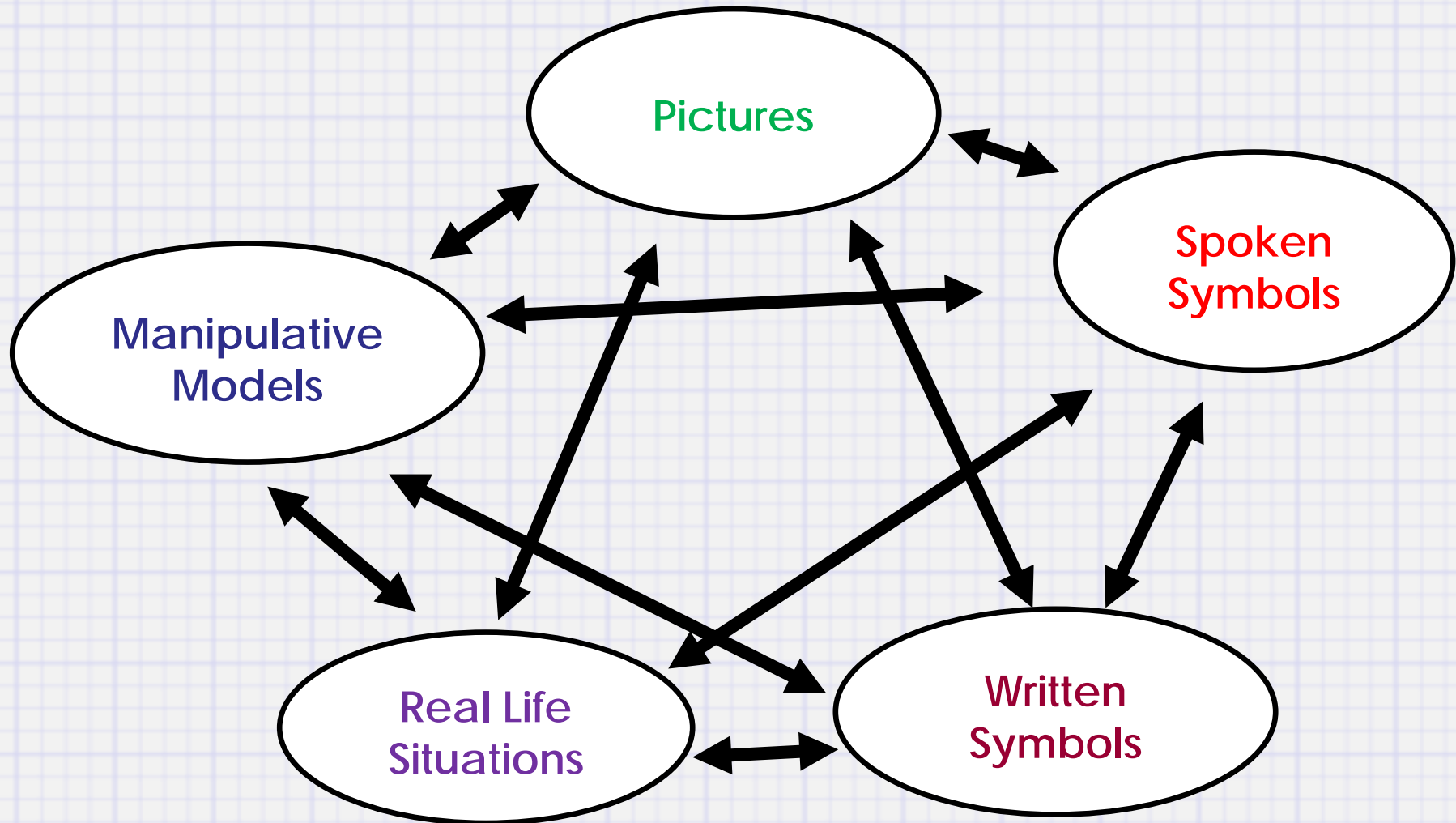
Spoken  
Symbols

Manipulative  
Models

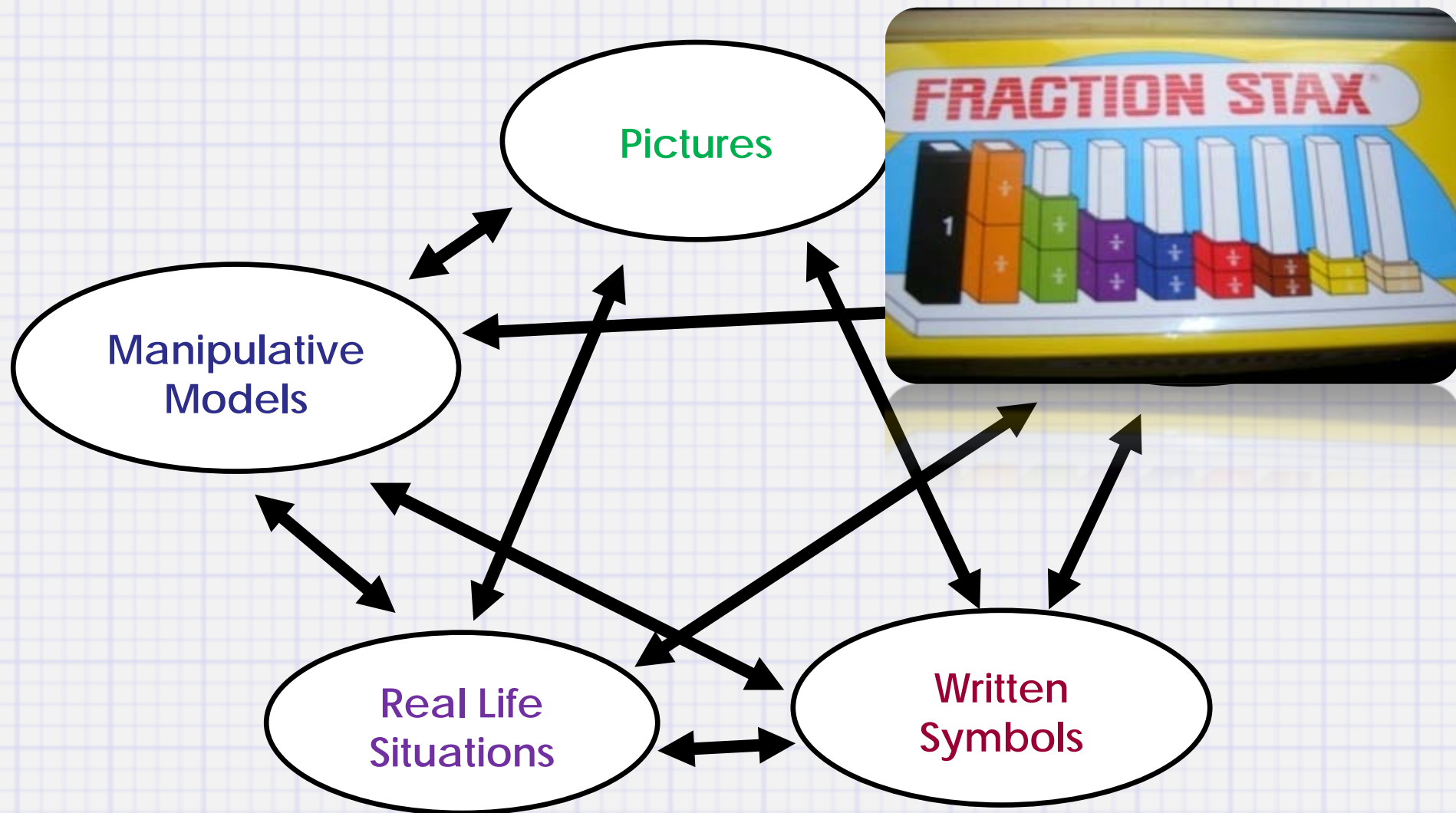
Real Life  
Situations

Written  
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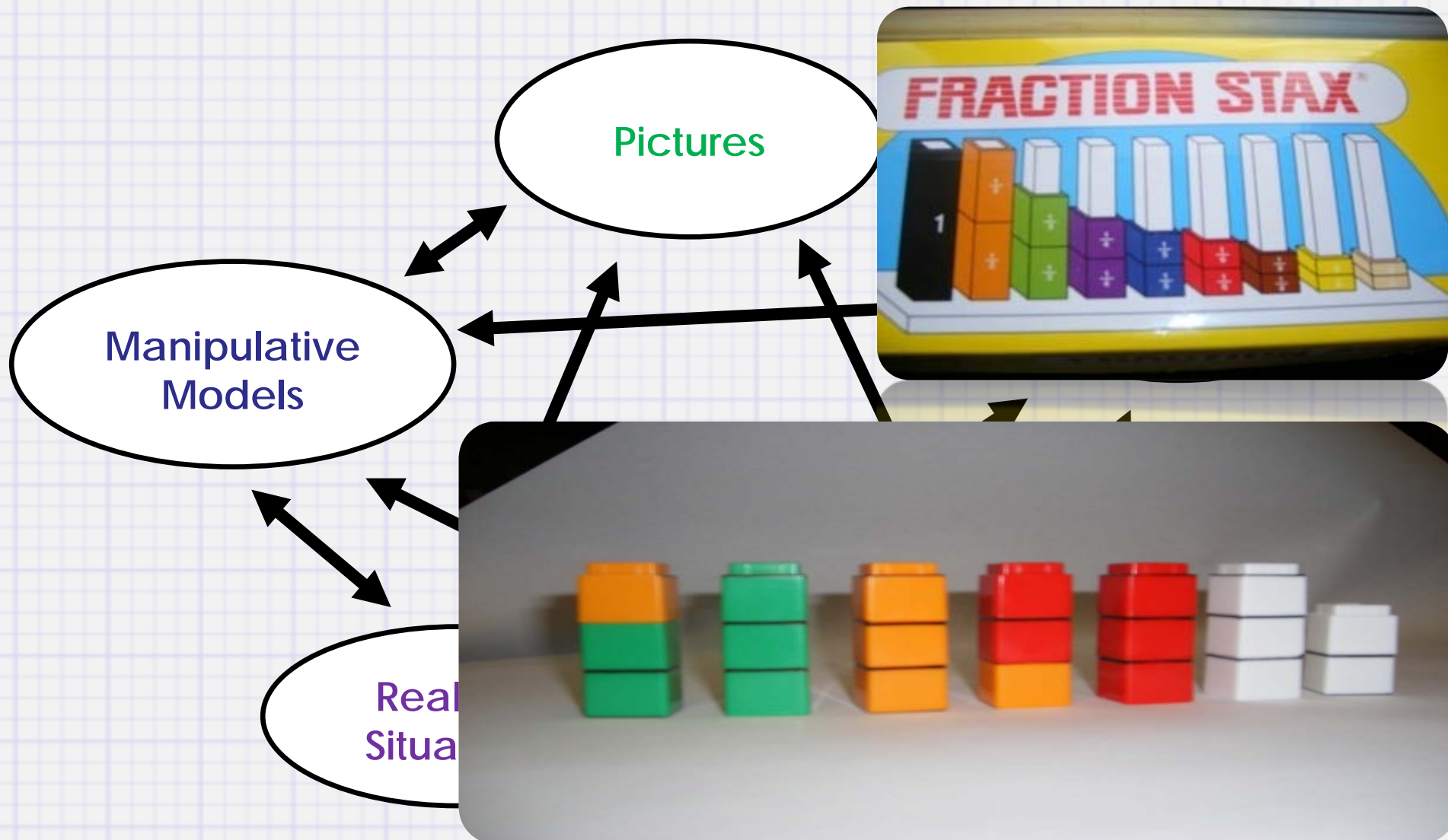
# Lesh's Translation Model



# Lesh's Translation Model



# Lesh's Translation Model



# Unifix Cubes

Cara has 4 pizzas for her party.

She decides that a serving will be  $\frac{3}{5}$  of a pizza.

Will she get  $6\frac{2}{3}$  or  $6\frac{2}{5}$  servings from the 4 pizzas?



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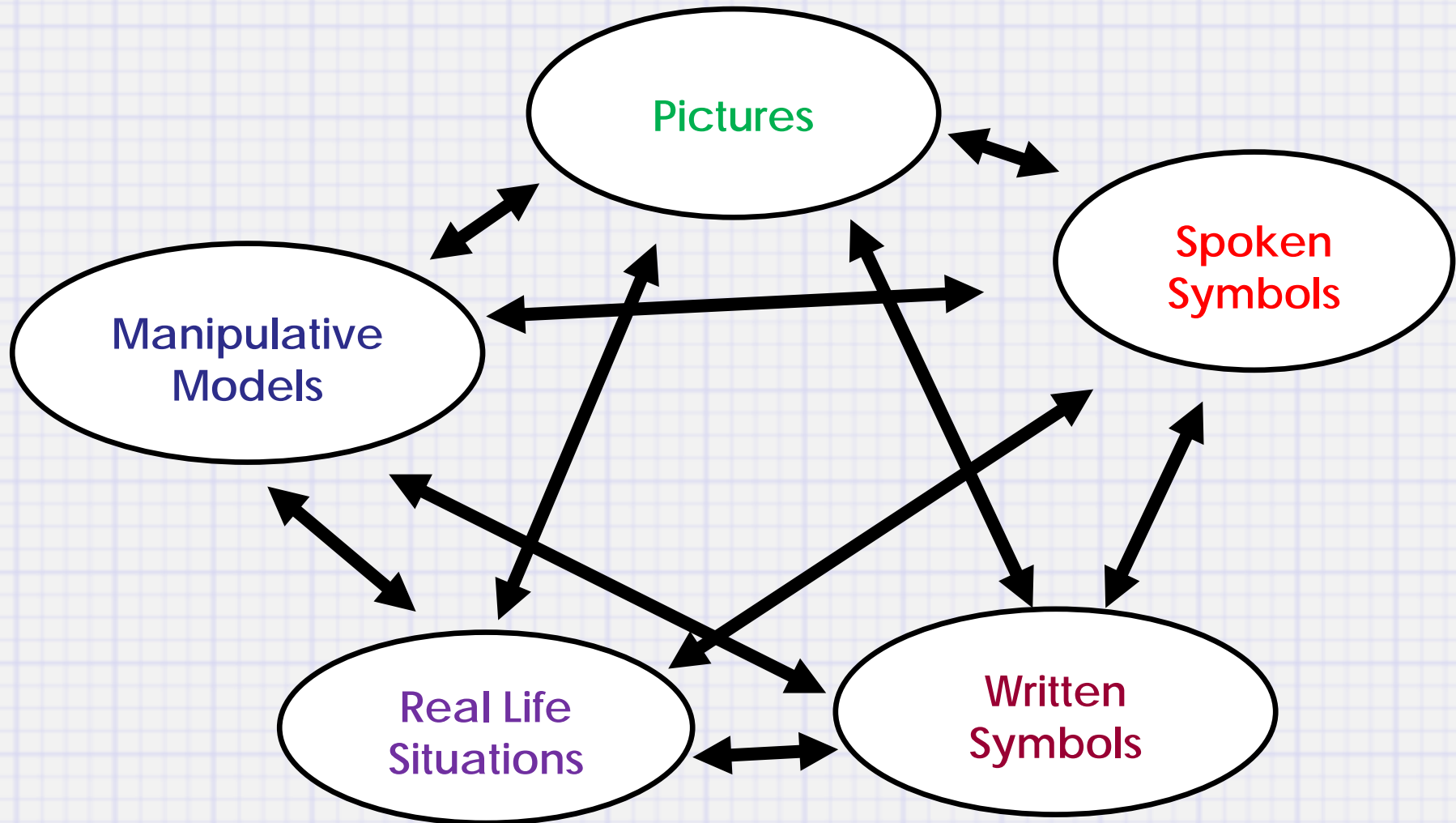
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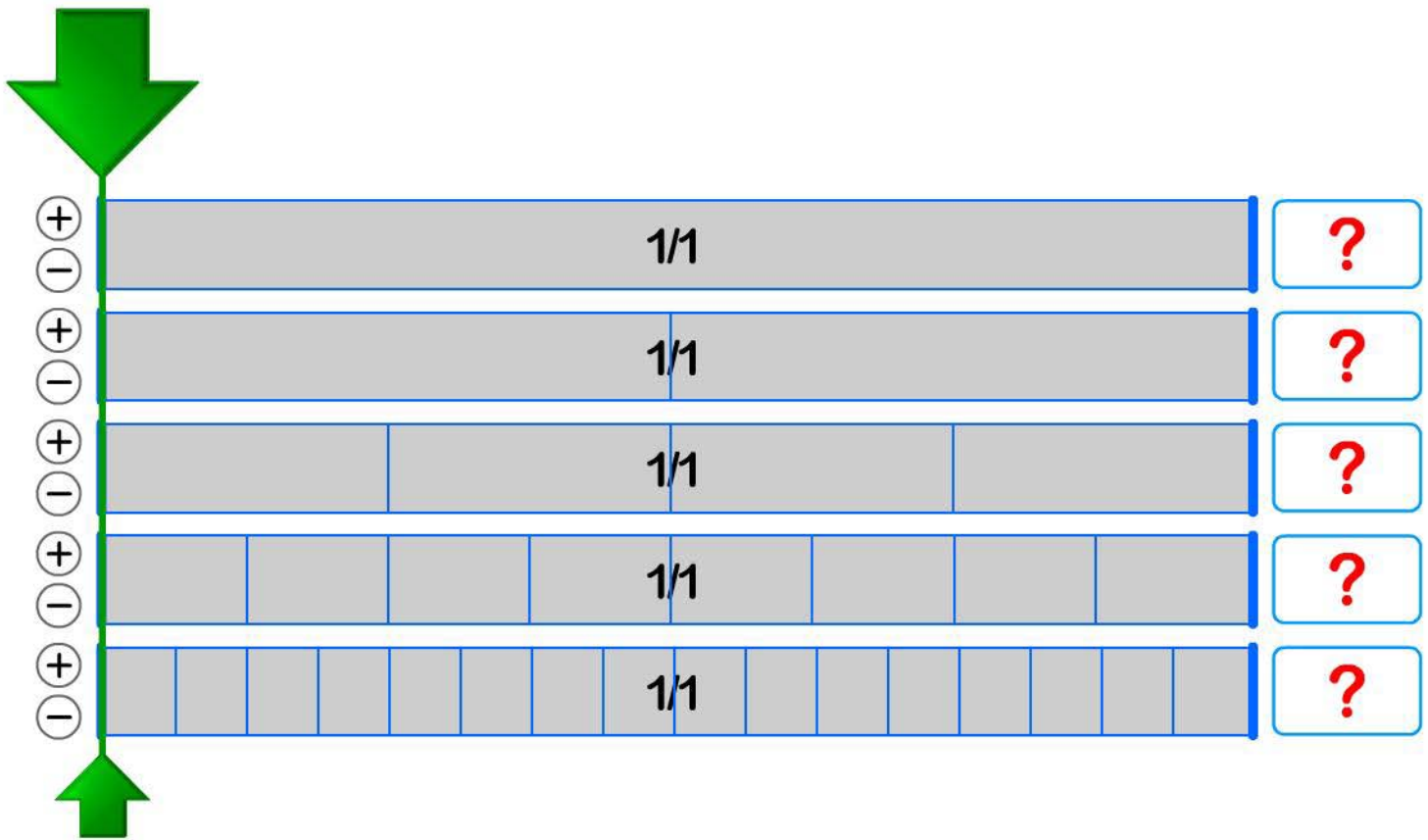




# Lesh's Translation Model



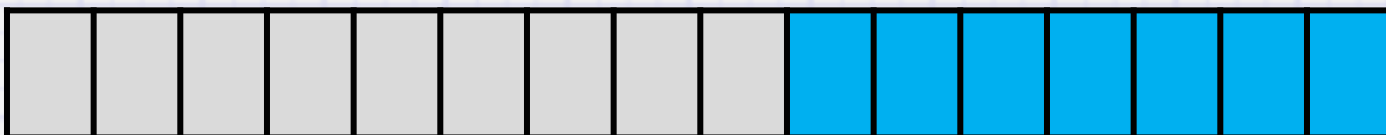
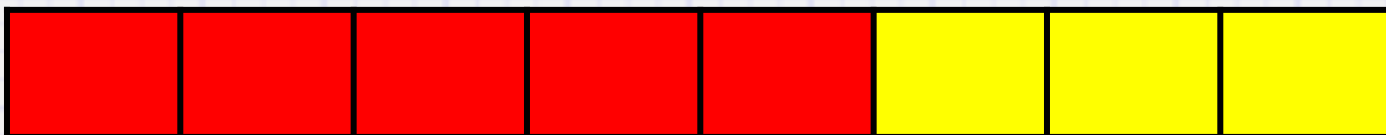
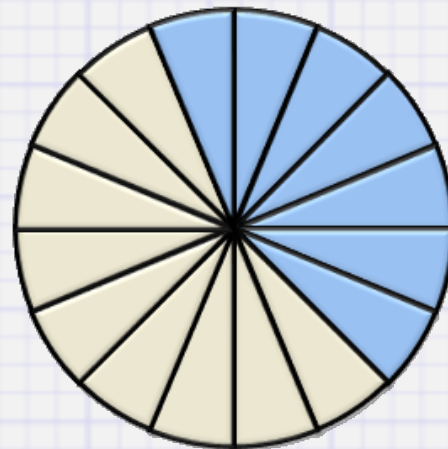
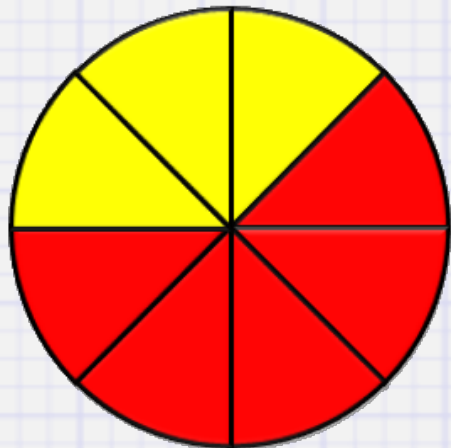
# Fraction Wall



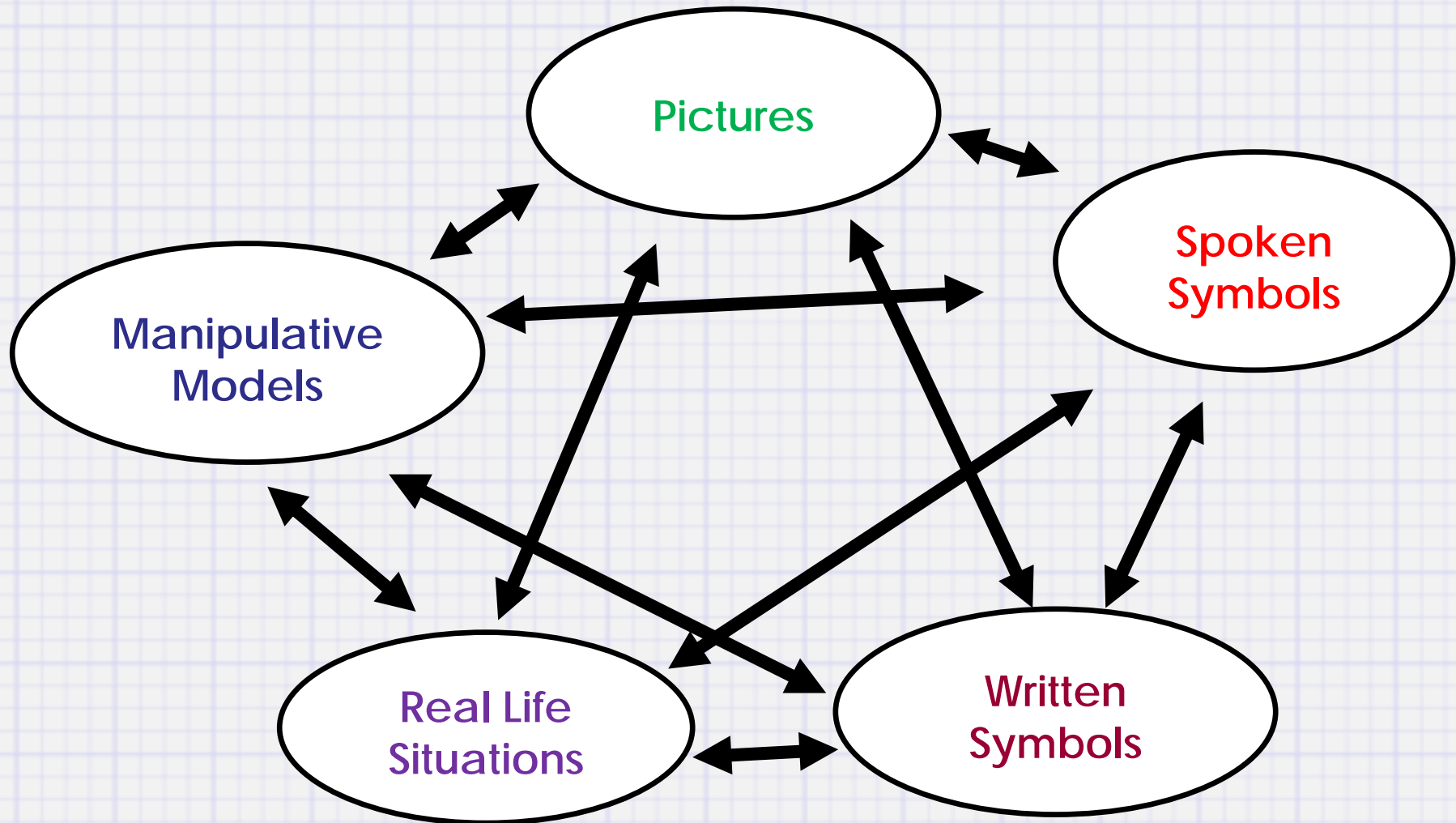
ROWS 5 Show labels

- Fractions
- Percentage
- Decimal
- Ratio

# Fraction Strips & Fraction Circles



# Lesh's Translation Model



# Overview of Fractions

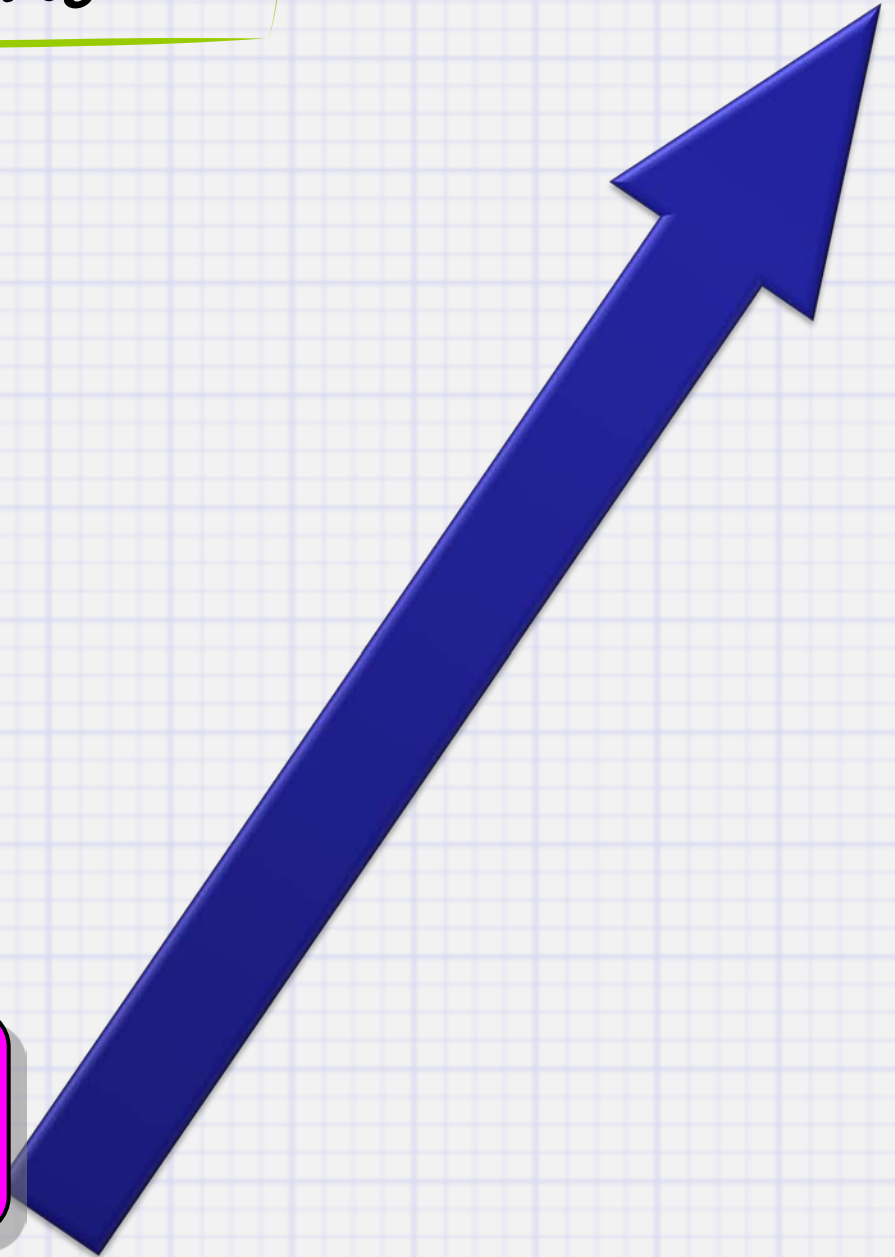
Prior  
knowledge



# Overview of Fractions

Prior  
knowledge

Diagnostic  
Test

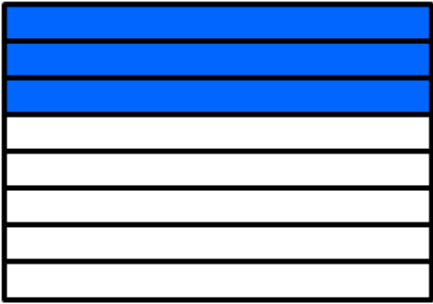


# Diagnostic Test

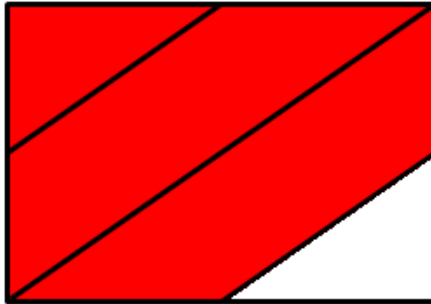
Which of these rectangles has  $\frac{3}{4}$  shaded in?

Is it more than one rectangle?

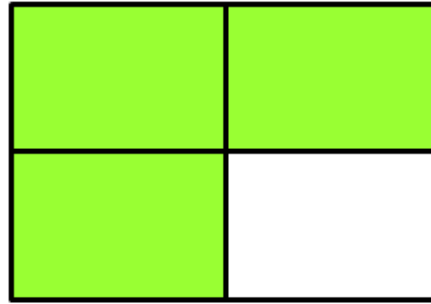
A.



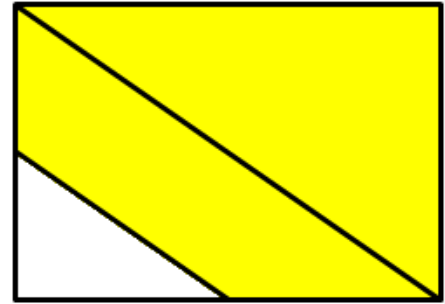
B.



C.



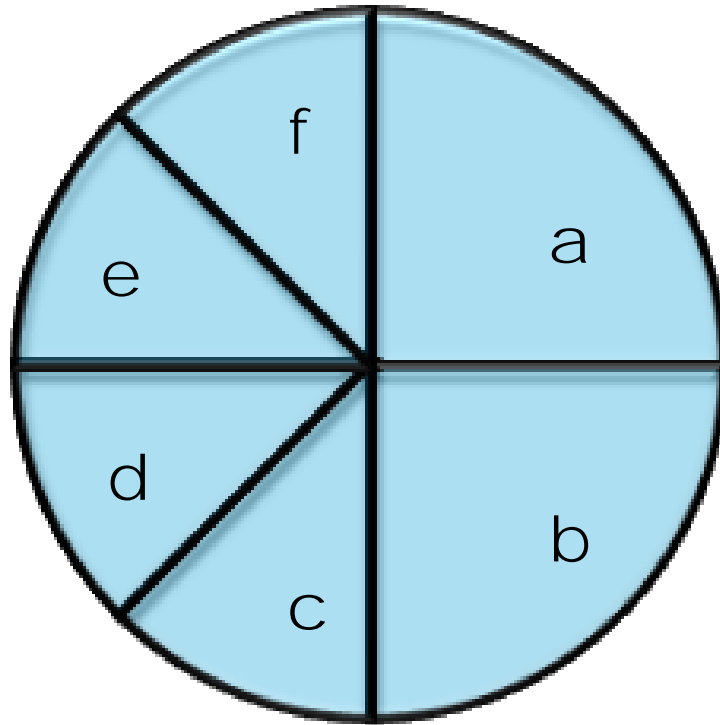
D.



Answer:

# Diagnostic Test

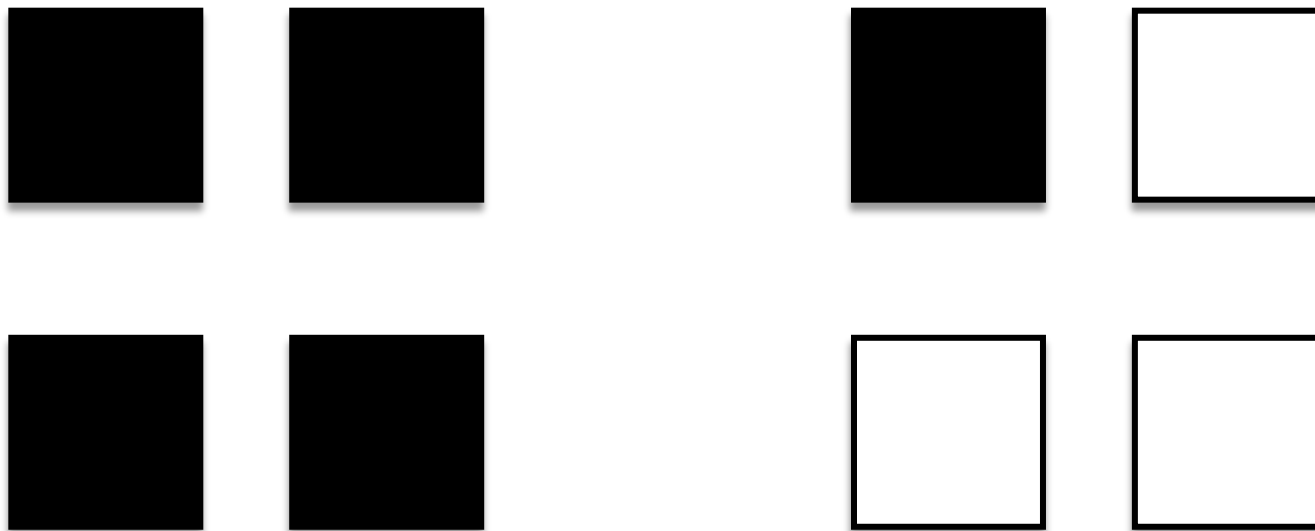
What fraction of the fraction circle is marked 'f'?



Answer:



# Diagnostic Test



The shaded part of this diagram could represent the numbers:

- (a) 5      (b)  $2\frac{1}{2}$       (c)  $\frac{5}{8}$       (d)  $1\frac{1}{4}$

Identify the unit in each case by drawing:

- (a)                      (b)                      (c)                      (d)

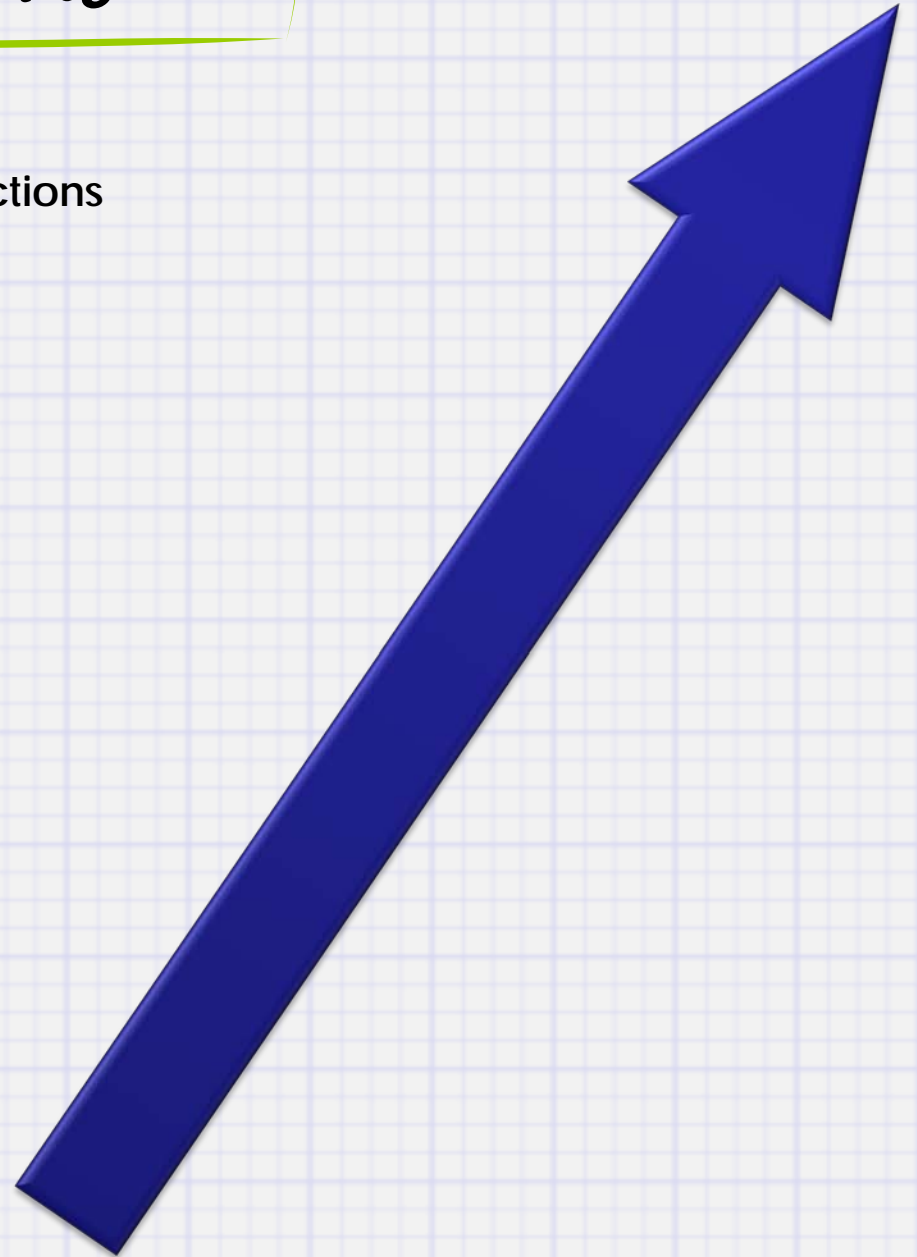
# Overview of Fractions

Connections

Operations

Concepts

Prior  
knowledge



# Overview of Fractions

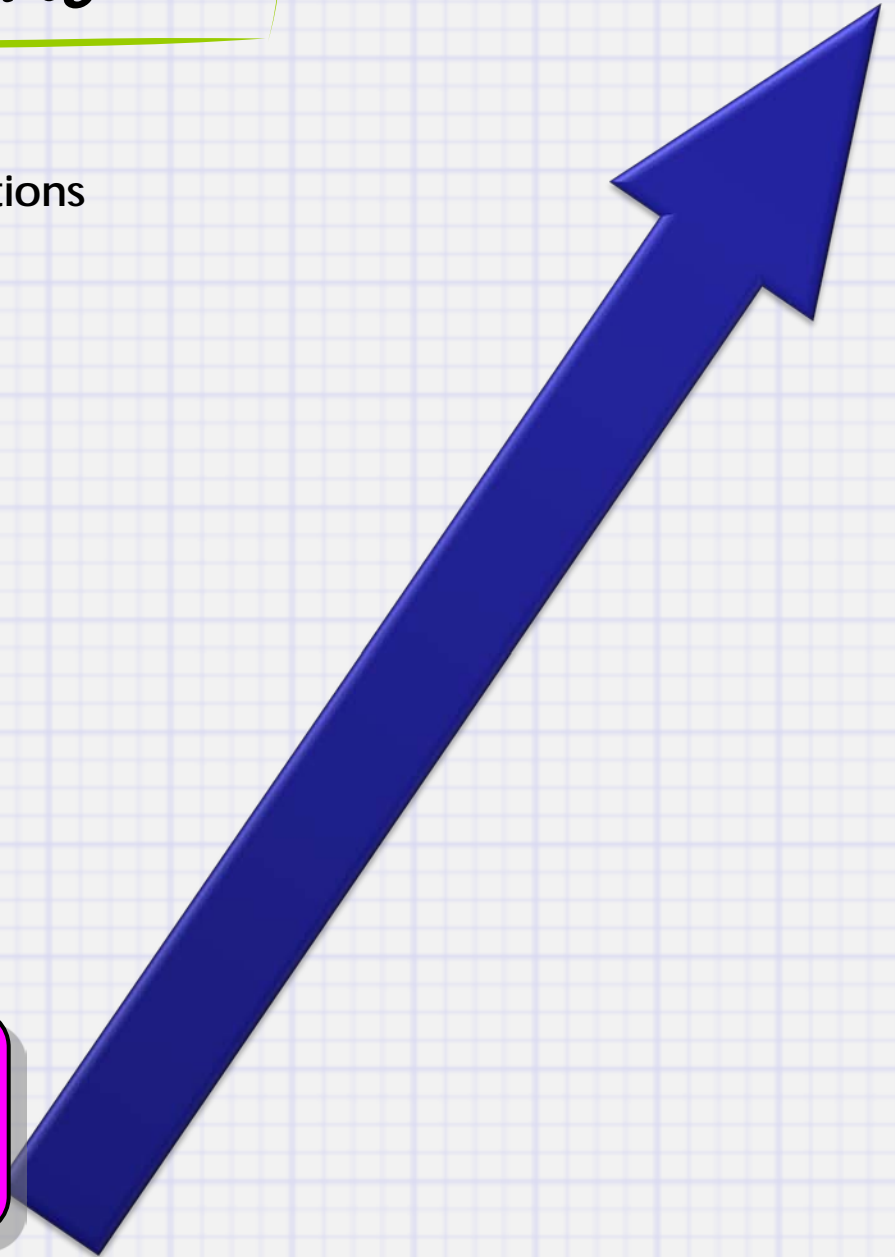
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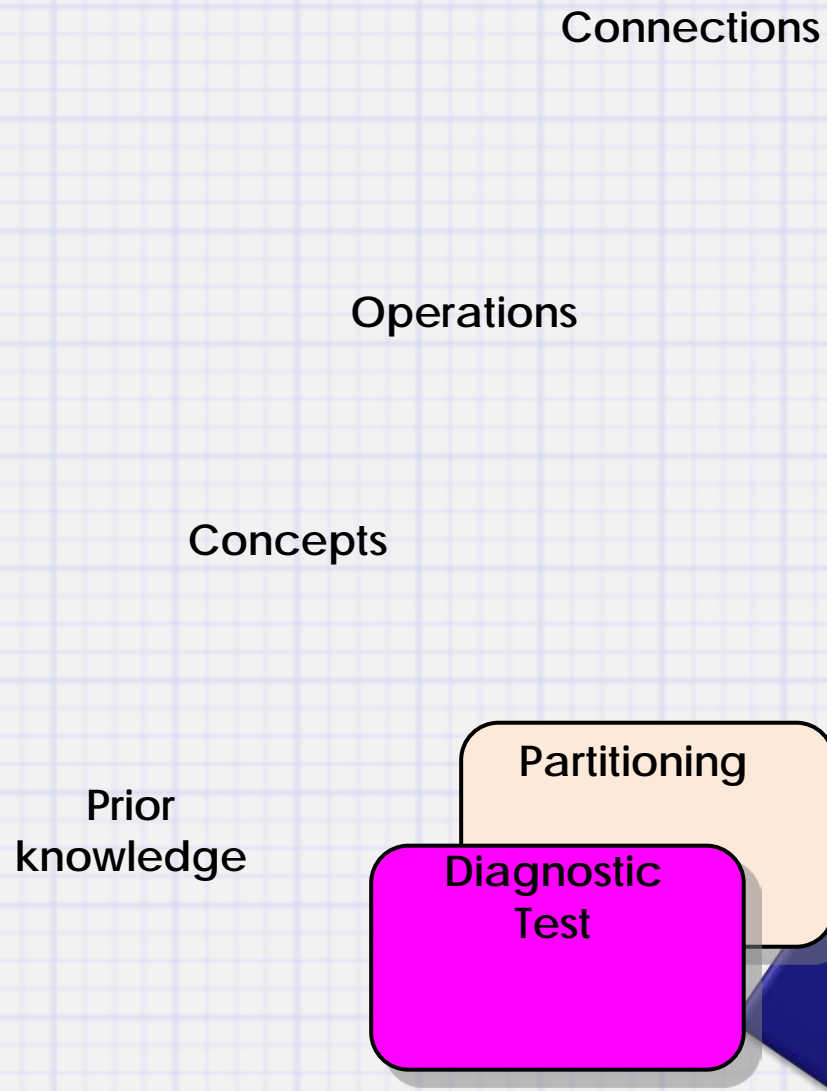
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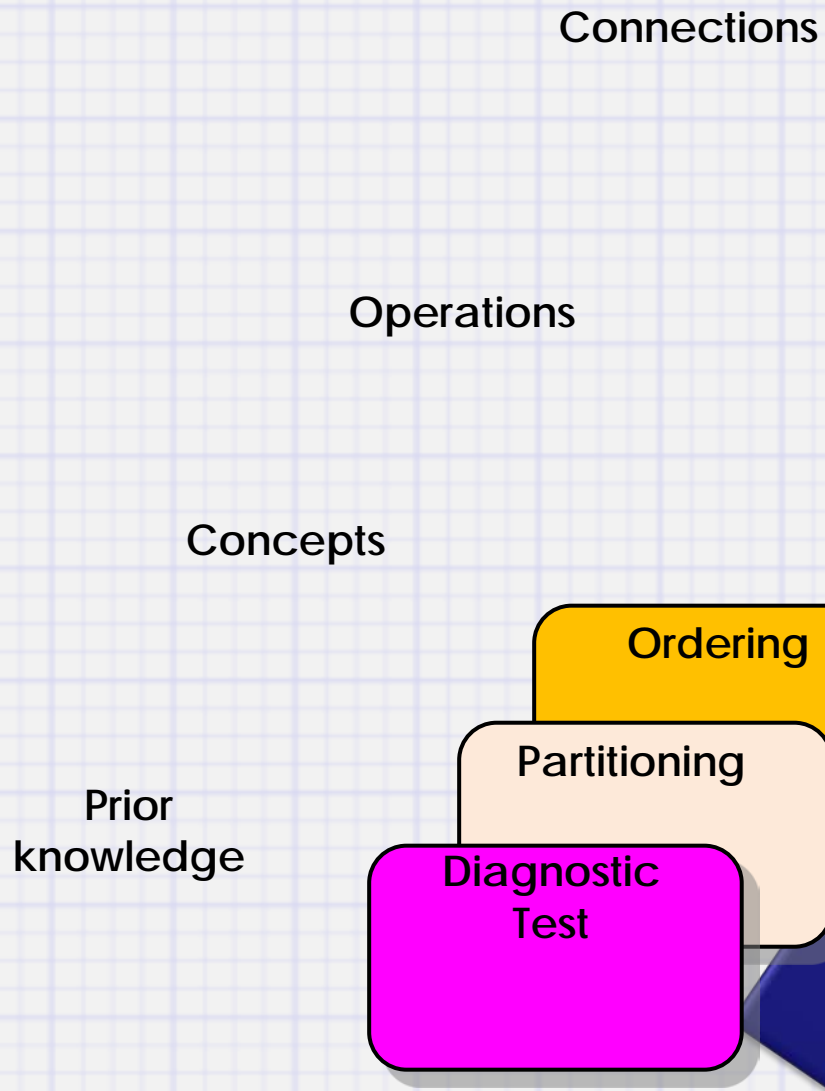
Diagnostic  
Test



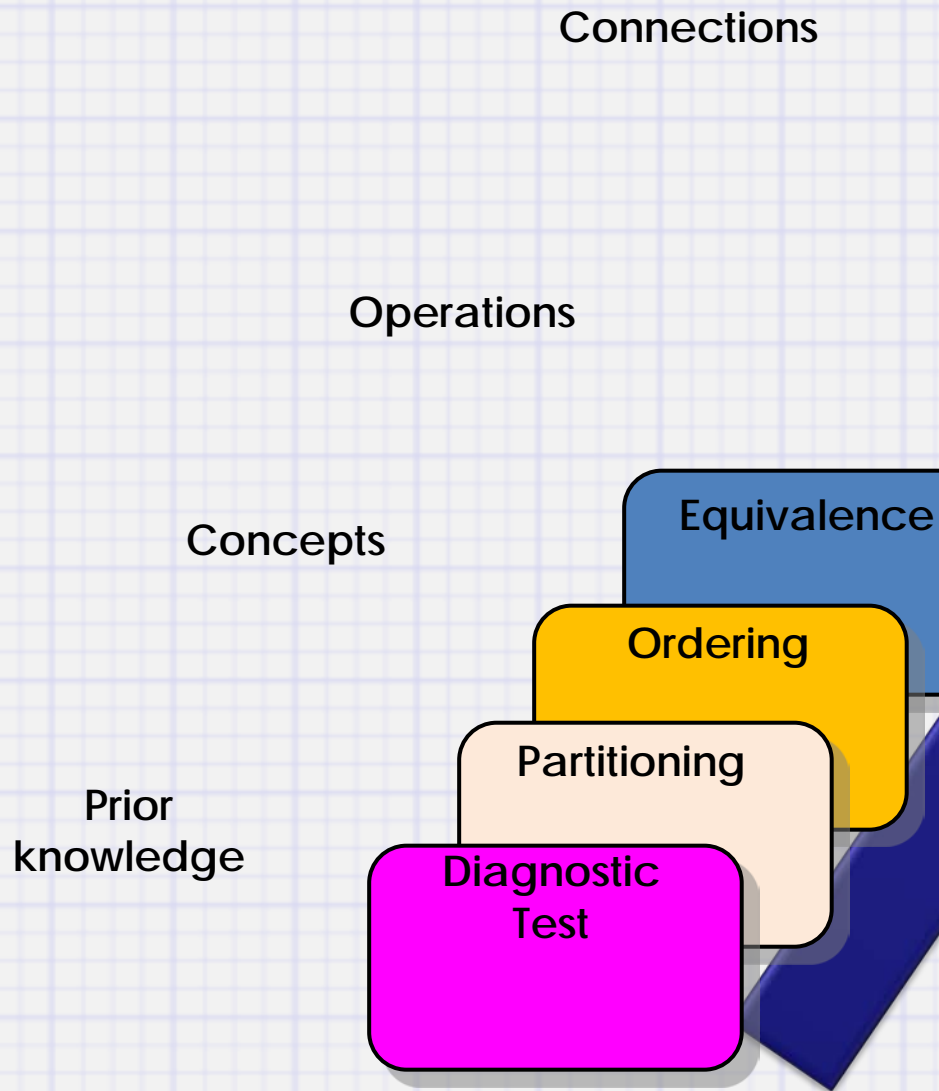
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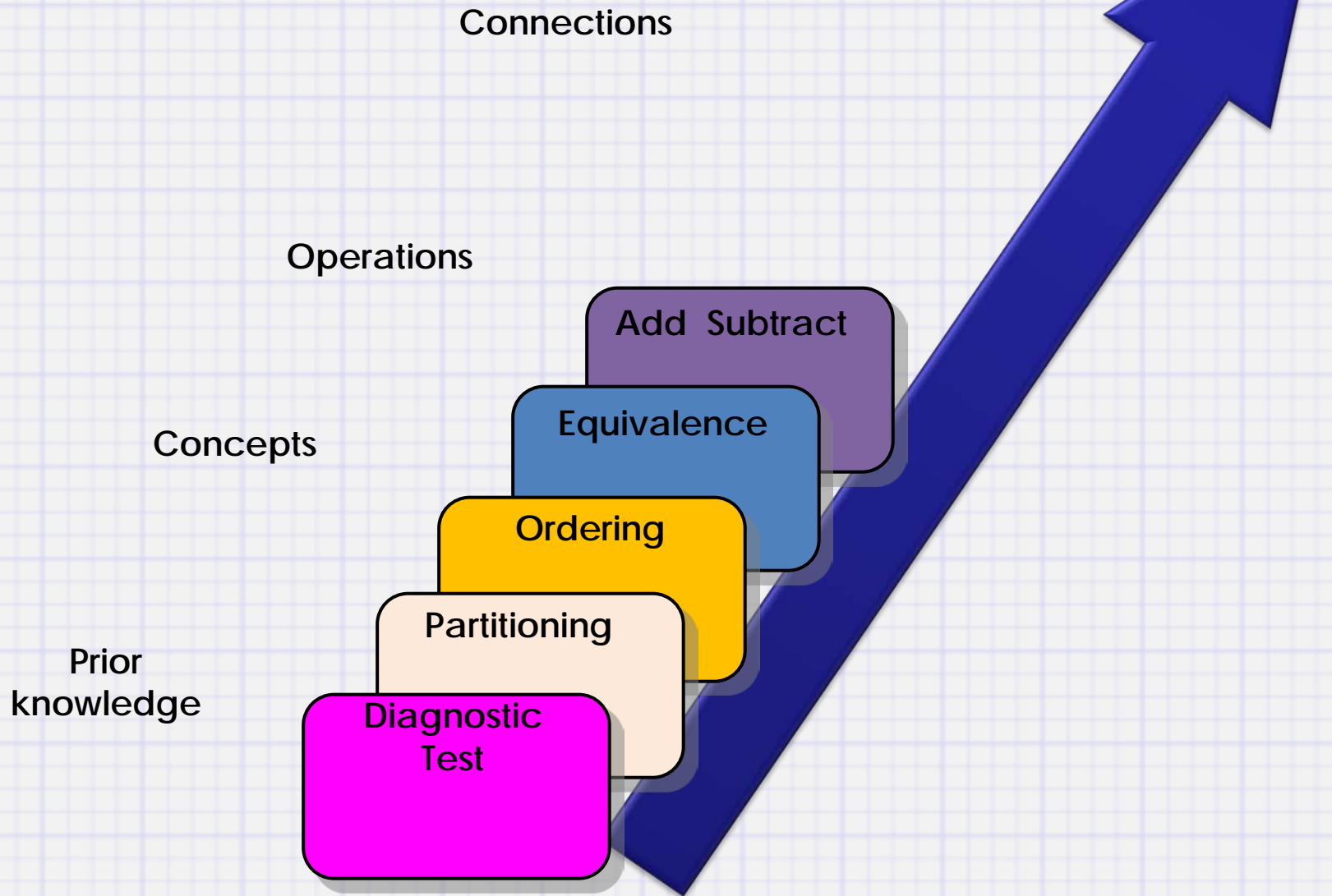
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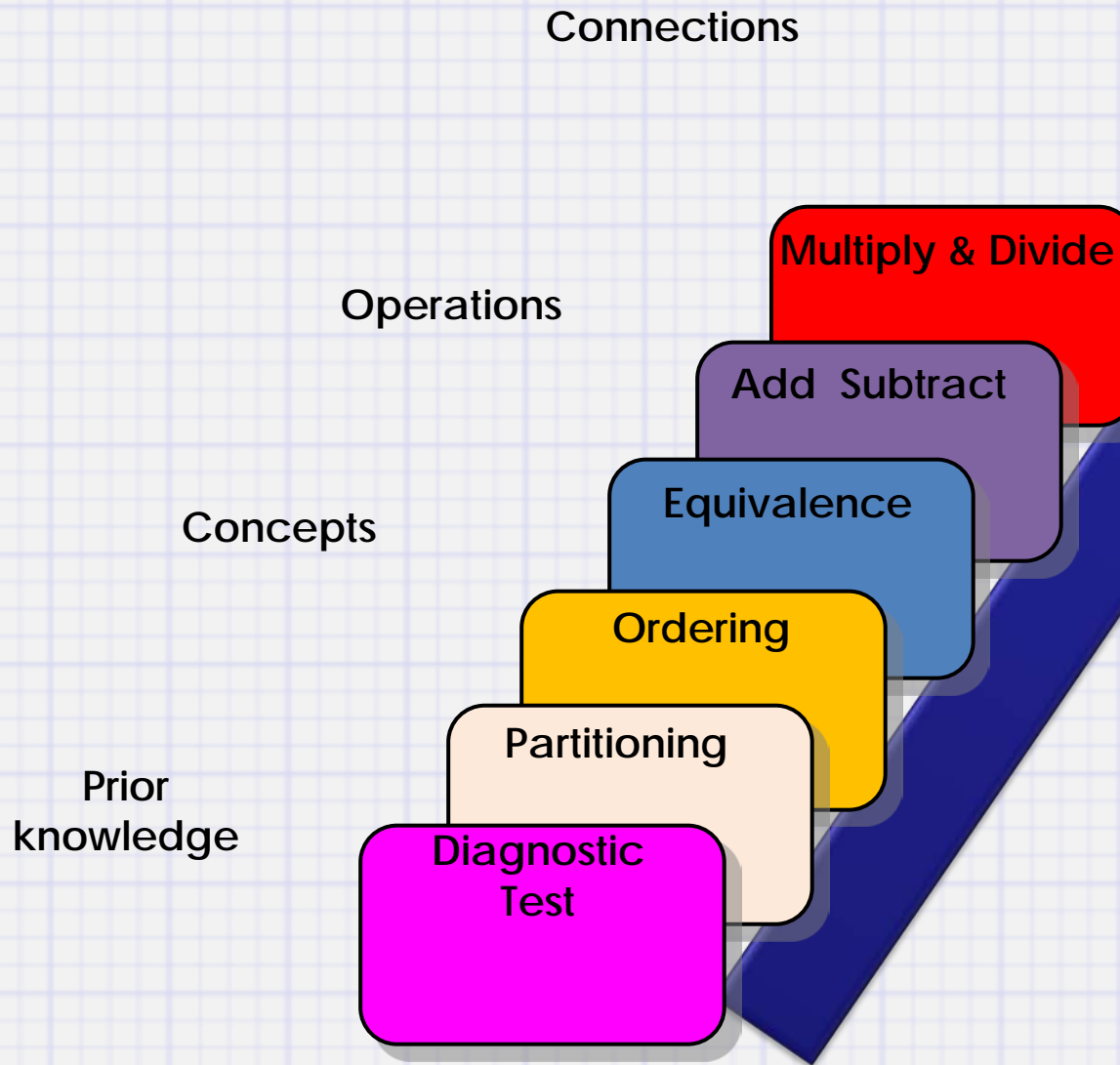
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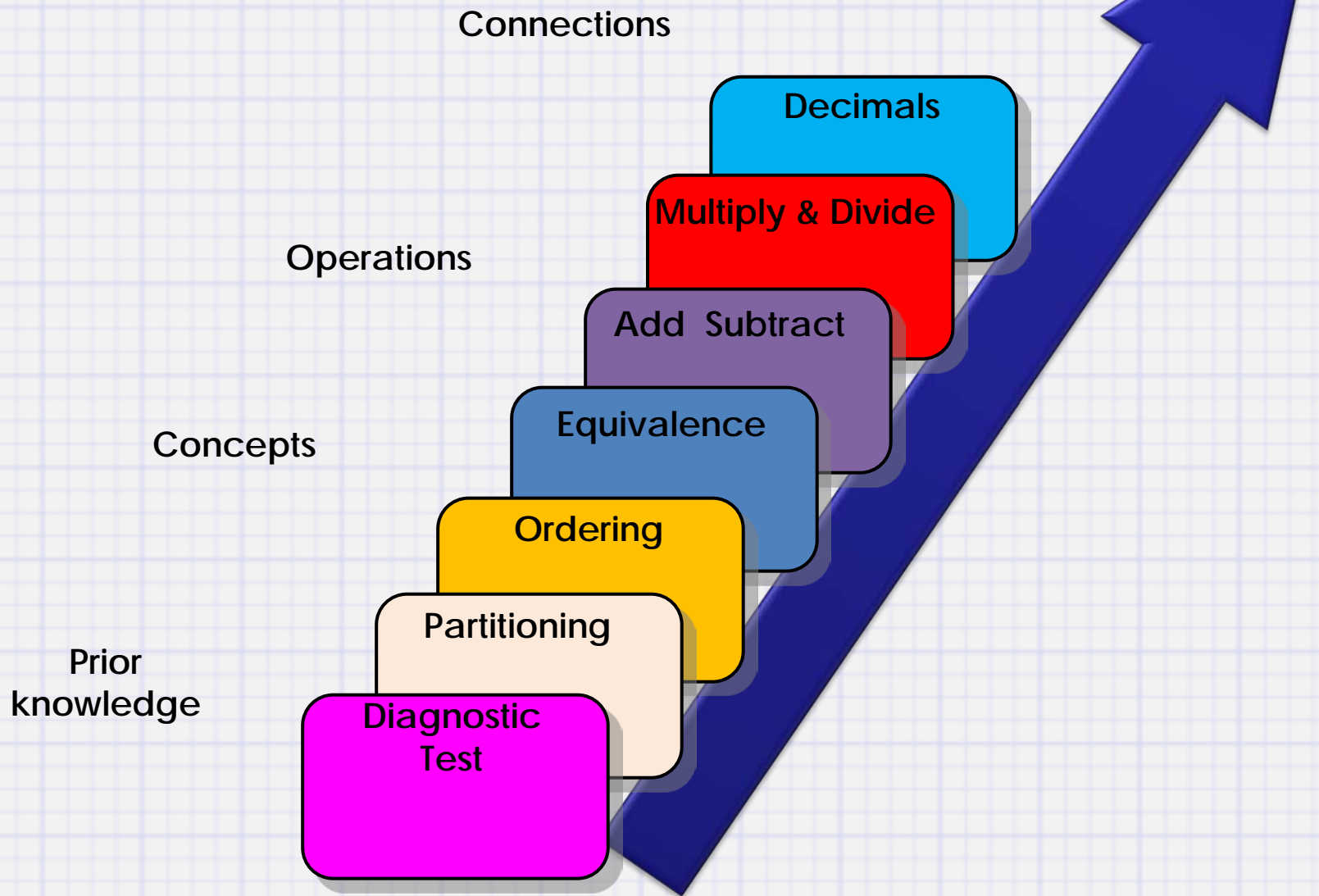


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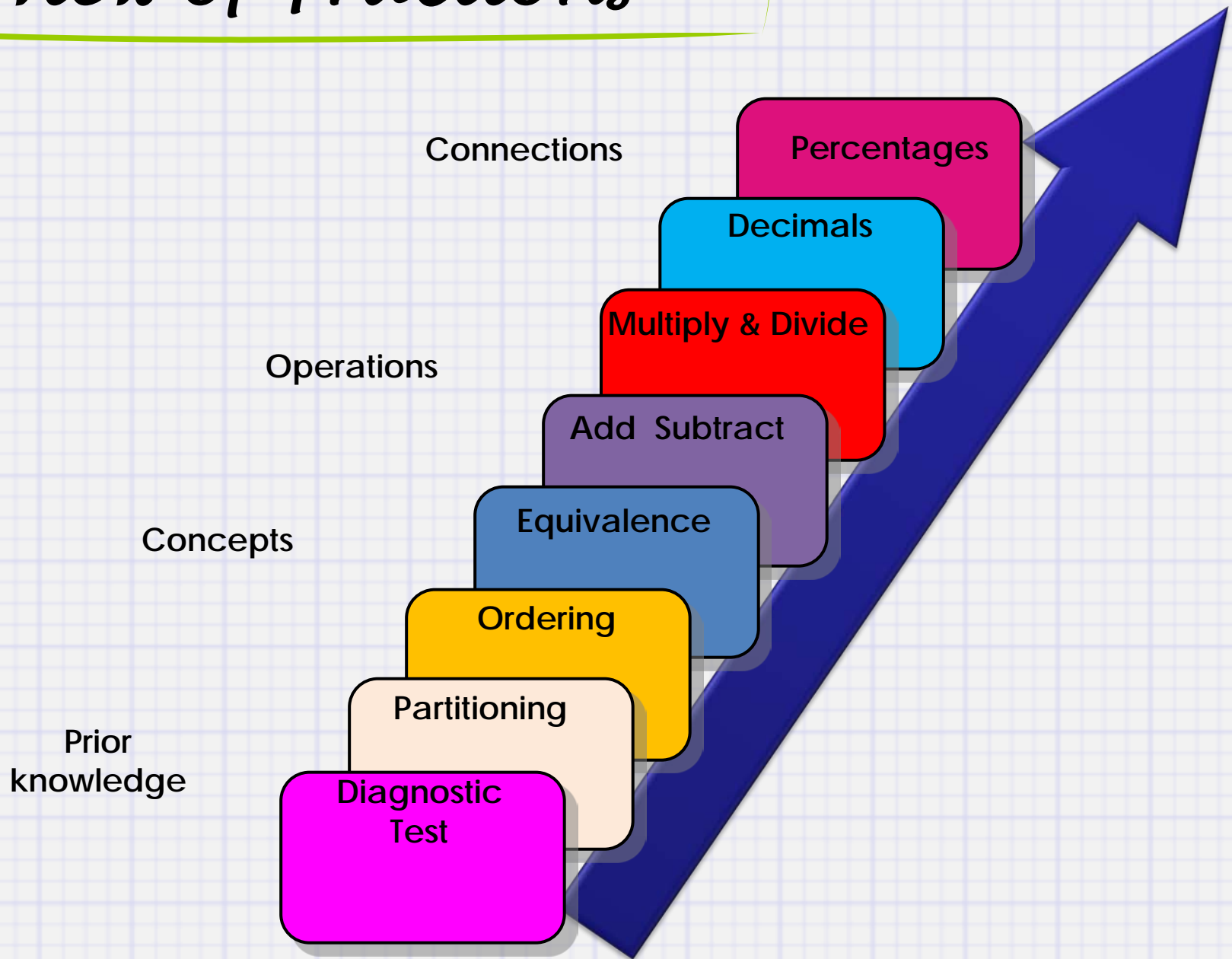




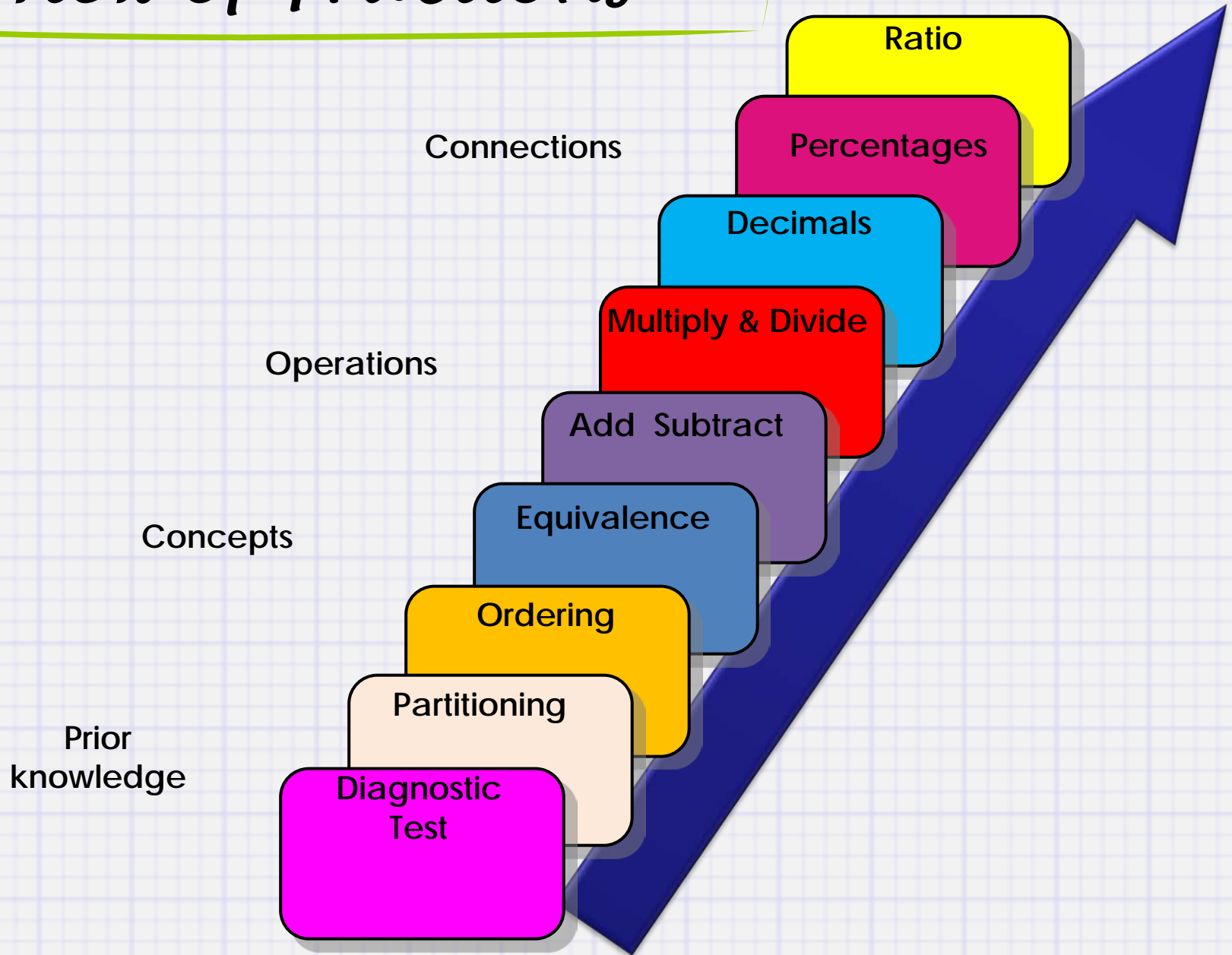
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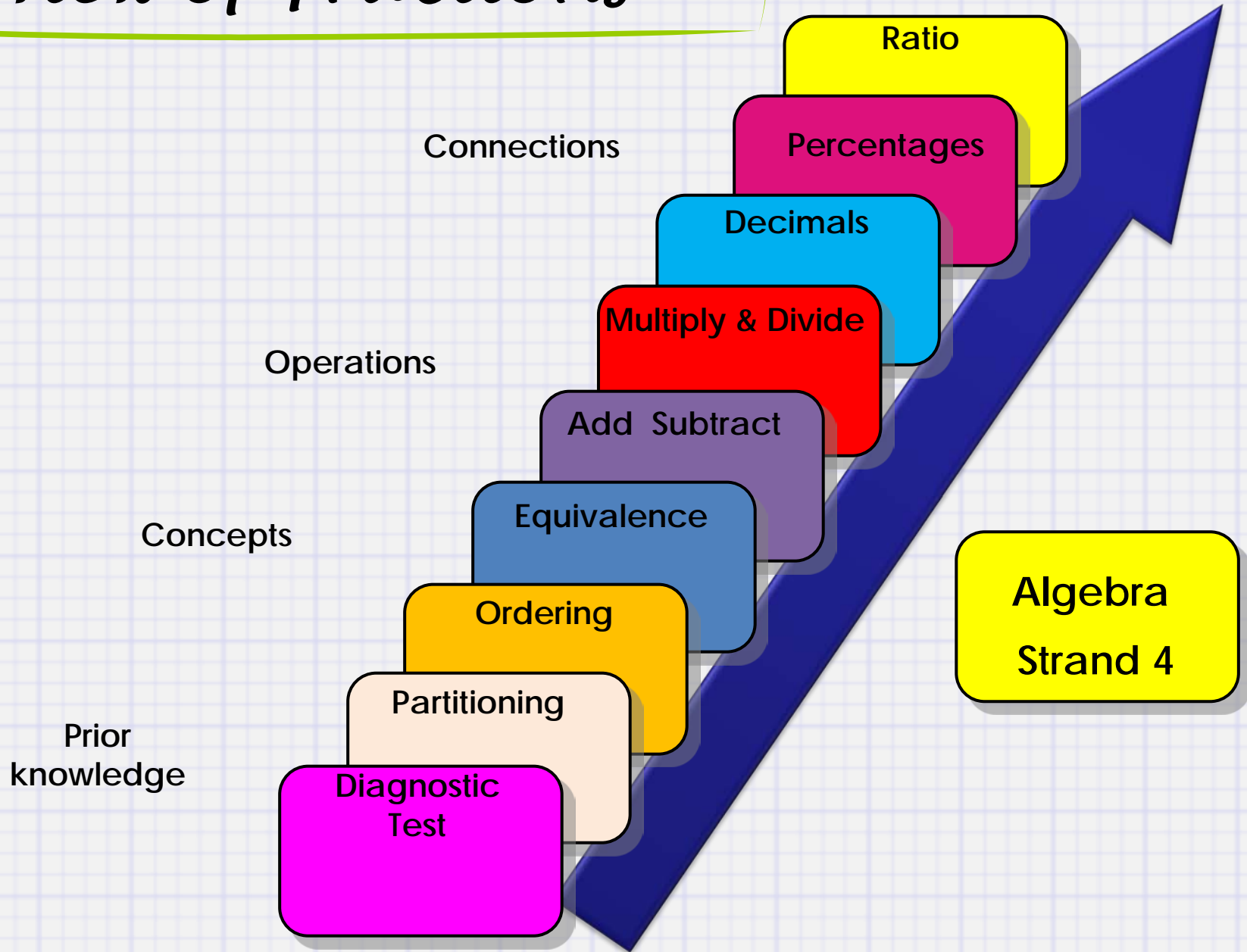
# Overview of Fractions



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# Overview of Fractions



# Concepts

- Partitioning
  - Ordering
    - Equivalence

*Reasons for rules ~  
Checking tools*

# Concepts

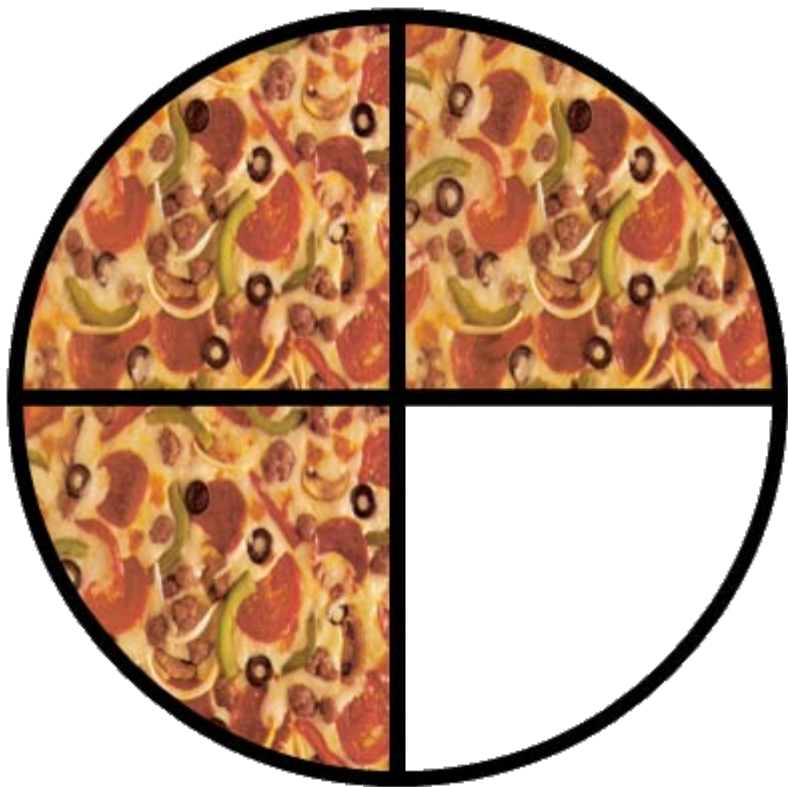
Is  $\frac{3}{4}$  always the same?

# Concepts

Is  $\frac{3}{4}$  always the same? *Only if the **unit** is the same.*

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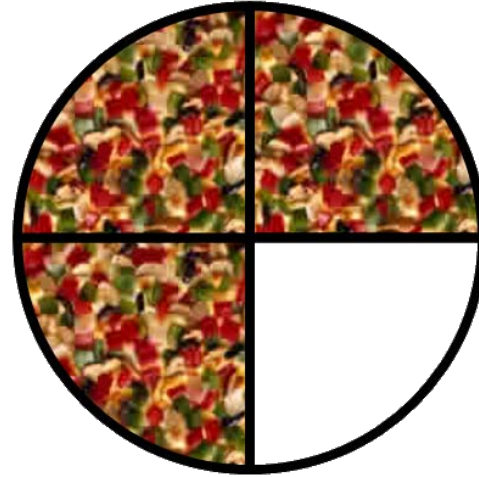
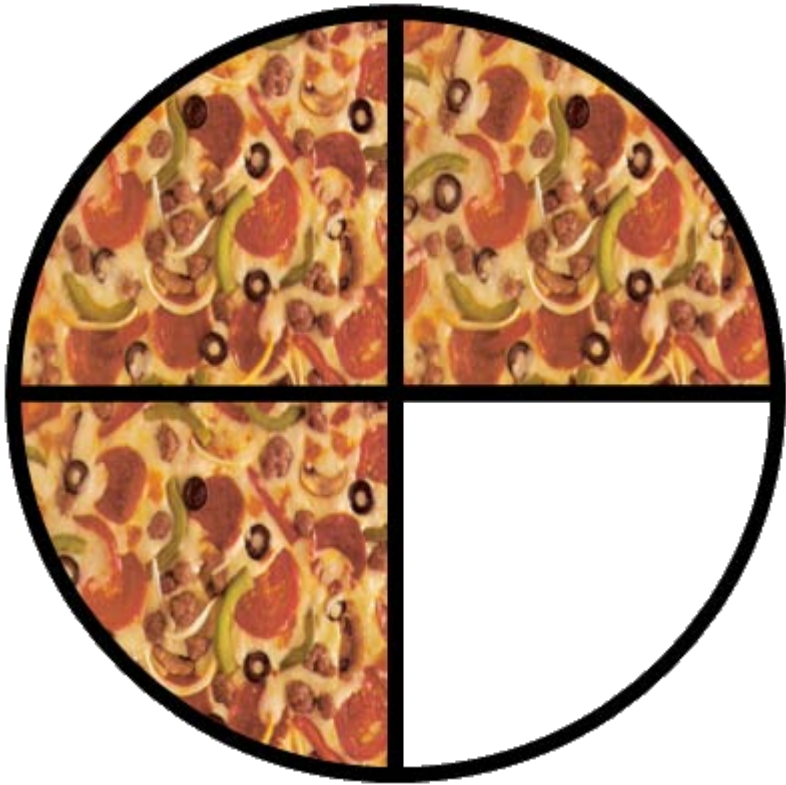
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# Concepts

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# Concepts

Which is bigger:  $\frac{3}{7}$  or  $\frac{5}{7}$ ?

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# Concepts

Which is bigger:  $\frac{3}{5}$  or  $\frac{2}{3}$ ?



# Whole Number Multiplication



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# *Whole Number Multiplication*

Liz wants to give each of her 3 friends 4 bars of chocolate. How would you work out how many bars she needs?

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- 3 groups of 4

# Multiplying a Whole Number by a Fraction

Barry is having 4 of his friends over to his house for pizza.

He is going to give them  $\frac{2}{3}$  of a pizza each.

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- (b) Draw a picture to model this situation.
- (c) If you have "4 groups of  $\frac{2}{3}$ ", how many 'one thirds' do you have?

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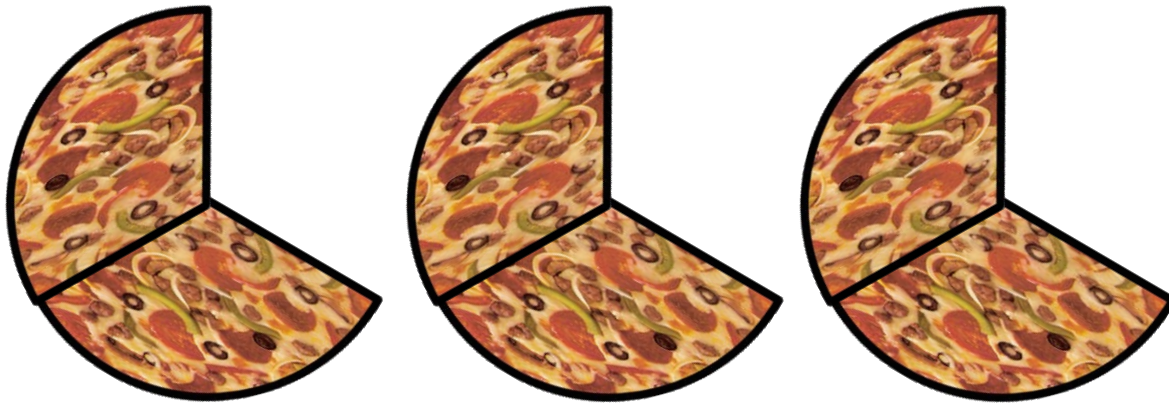


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# Poster/ White Boards

- Picture/Words
- Multiplication sentence
- ...groups of...
- Repeated addition

# Pair Work

If I multiply  $4 \times \frac{2}{3}$  what **incorrect answer** do you think I might get?



# Pair Work

How come

$$\left\{ \begin{array}{l} \frac{4}{1} \times \frac{2}{3} = \frac{8}{3} \text{ and} \\ \frac{4}{1} + \frac{2}{3} = 4\frac{2}{3} ? \end{array} \right.$$

# Fraction $\times$ Fraction

Cara has  $\frac{2}{5}$  of her rectangular birthday cake left over from her party.

She ate  $\frac{3}{4}$  of the leftover cake.

How much of the full cake was this?

